

Particle Morphology and Lithium Segregation to Surfaces of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ Solid Electrolyte

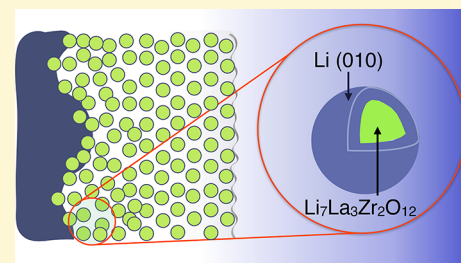
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S Supporting Information

ABSTRACT: Solid electrolytes for solid-state Li-ion batteries are stimulating considerable interest for next-generation energy storage applications. The $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ garnet-type solid electrolyte has received appreciable attention as a result of its high ionic conductivity. However, several challenges for the successful application of solid-state devices based on $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ remain, such as dendrite formation and maintaining physical contact at interfaces over many Li intercalation/extraction cycles. Here, we apply first-principles density functional theory to provide insights into the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particle morphology under various physical and chemical conditions. Our findings indicate Li segregation at the surfaces, suggesting Li-rich grain boundaries at typical synthesis and sintering conditions. On the basis of our results, we propose practical strategies to curb Li segregation at the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ interfaces. This approach can be extended to other Li-ion conductors for the design of practical energy storage devices.



INTRODUCTION

The commercial Li-ion battery, which relies on liquid electrolytes, is now the workhorse behind the mobile electronics industry.^{1–5} Unfortunately, a practical limit of what can be achieved with the current Li-ion technology is encountered when the focus shifts to electric vehicles.^{2,4–6} One promising avenue to improve the energy and power densities of Li-ion batteries, while enhancing their safety, consists of replacing the flammable liquid electrolyte with a solid electrolyte capable of efficiently shuttling Li ions between electrodes.^{7–21}

To facilitate this transition, the Li-ion conductivity of solid electrolytes must be competitive to that of their liquid analogs.^{12,16} While significant attention is still devoted to intrinsic Li^+ conductivity in solid electrolytes, many challenges remain for future solid-state applications.^{5,22–30} The most pressing challenges are finding solid electrolytes that are electrochemically stable against electrodes, maintaining physical contact between components over many Li intercalation/extraction cycles and suppressing Li-dendrite formation.

The $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ garnet-type electrolyte has received significant attention due to its high ionic conductivity (10^{-6} – 10^{-3} S cm^{-1}) achieved by a variety of doping strategies^{7,8,10,11,31–36} but also because of its perceived stability against the Li-metal anode.^{25,27,29,37–41}

However, the failure of polycrystalline $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ in solid-state battery prototypes comprising Li-metal anodes has been the subject of several studies.^{25,28,38,40–43} It has been observed²⁹ that once Li fills a crack in the $\text{Li}_6\text{La}_3\text{ZrTaO}_{12}$ polycrystalline material, fresh electrodeposited Li is extruded to the available surface. Tests with Li-metal/ $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ /Li-metal cells

showed that only small current densities of ~ 0.5 mA cm^{-2} could be tolerated before dendrite failure.^{27,44} Rationalizing the mechanisms behind the propagation of dendrites in $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ is a major challenge.

In parallel, sintering strategies to maximize the bulk transport in ceramic materials are routinely applied. While high temperature densification enhances ion transport, the extent of morphological transformations of the electrolyte particles is still unclear. Kerman et al.²⁷ highlighted the connection between the processing conditions of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ and its particle morphology and size. Kingon et al.⁴⁵ demonstrated that ceramics containing volatile cations, such as $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, become Li deficient upon sintering. These experimental observations indicate that it is crucial to understand the variation of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ morphology as a function of chemical and physical properties (such as composition and temperature).

In this study, we develop a phenomenological model based on first-principles calculations to determine the composition of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles, while the chemical environment of Li, La, Zr, and O, the voltage, and/or the temperature are varied. Rationalizing the particle morphology of solid electrolytes contributes toward a deeper understanding of several critical phenomena, including the Li^+ conductivity at grain boundaries and the propagation of dendrites during battery operation. Indeed, our results predict significant Li accumulation at the

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exterior of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles when we mimic high-temperature synthesis conditions.

On the basis of our computational insights, we propose practical strategies to engineer the chemical compositions of the particles, providing a greater control of the complex chemistry of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. These general design strategies can be extended to other solid electrolytes and electrode materials.

RESULTS

Phase Stability and Chemical Domains. We first consider the relative stability of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ tetragonal (space group $I4_1/acd$) and high-temperature cubic ($Ia\bar{3}d$) polymorphs. The computed lattice constants ($a = 13.204$ and $c = 12.704$ Å) of the tetragonal phase compare well with the experimental data ($a = 13.134$ and $c = 12.663$ Å).⁴⁶

Figure 1a shows the decomposition of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ into $\text{Li}_6\text{Zr}_2\text{O}_7 + \text{La}_2\text{O}_3 + \text{Li}_8\text{ZrO}_6$, revealing the metastability of both

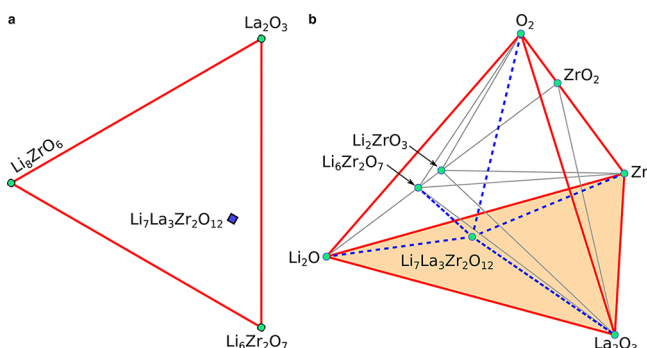


Figure 1. (a) La_2O_3 – $\text{Li}_6\text{Zr}_2\text{O}_7$ – Li_8ZrO_6 projection of the quaternary Li–La–O–Zr phase diagram showing the decomposition products of the metastable $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ (blue diamond), which are $\text{Li}_6\text{Zr}_2\text{O}_7$, La_2O_3 , and Li_8ZrO_6 . (b) Compound Li_2O – La_2O_3 – Zr – O_2 phase diagrams, where $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ is assumed to be stable. Green dots display the stable phases, while red, blue, and gray lines identify equilibrium tie lines. Dash blue lines mark tie lines shared by $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ and some of the binary precursors used in its synthesis. Both phase diagrams are computed from DFT data at 0 K and combined with existing entries in the Materials Project database.⁴⁹

the cubic (~ 22 meV/atom above the stability line at 0 K) and tetragonal (~ 7 meV/atom) polymorphs, in agreement with previous density functional theory (DFT) predictions.^{47,48}

The degree of metastability of the tetragonal phase is small enough that the compound can be stabilized by thermal effects, which explains the success of high-temperature (>600 °C) phase-pure synthesis.^{8,11} It is assumed that the chemical decomposition of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ into $\text{Li}_6\text{Zr}_2\text{O}_7 + \text{La}_2\text{O}_3 + \text{Li}_8\text{ZrO}_6$ requires a major coordination rearrangement of Zr and La, thereby kinetically preventing $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ from decomposing. Therefore, we consider that $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ is thermodynamically stable (see phase diagram in Figure 1b).

Identifying the phases in equilibrium with $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ (Figure 1b) allows us to set the bounds of chemical potentials of each element, thus providing a thermodynamic framework to calculate meaningful surface energies of nonstoichiometric surfaces (see Method section). Figure 1b illustrates the phases in equilibrium with $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, which show that only La_2O_3 , $\text{Li}_6\text{Zr}_2\text{O}_7$, Li_2O , O_2 , and Zr are in direct equilibrium with the solid electrolyte. Experimentally, the binary compounds La_2O_3 , Li_2CO_3 (LiOH or Li_2O),²⁹ and ZrO_2 are used as precursors for the synthesis of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$.^{8,29} In addition, when

$\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ is assumed to be stable, Li_8ZrO_6 becomes metastable in the Li–La–Zr–O phase diagram (Figure 1b).

Our discussion moves to the relevant chemical potentials, which have to be rigorously defined to accurately calculate the energies of nonstoichiometric surface structures (see eq 1). From thermodynamic arguments, any combination of three compounds in equilibrium with $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ define distinct chemical potentials (μ) for the elements O, La, Li, and Zr. In this study, we consider two different chemical regimes, i.e., oxidizing and reducing. The tetrahedron composed of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, La_2O_3 , Li_2O , and O_2 mimics the oxidizing and experimental synthesis conditions of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. In contrast, we consider a reducing environment as defined by $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ being in equilibrium with Zr metal, La_2O_3 , and Li_2O , which corresponds to experimental sintering conditions. A detailed derivation and the bounds of the chemical potential used for each species are summarized in section 1 and Table S1 of the Supporting Information.

Although Zr forms oxides with multiple oxidation states, such as ZrO and Zr_2O as reported by Chen et al.,⁵⁰ Zr is not redox active in $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. Therefore, Zr-metal and ZrO_2 represent valid reference states for the μ_{Zr} in reducing (Zr^0) and oxidizing (Zr^{4+}) environments, respectively.

Surface Structures and Energies. Surfaces of solid electrolytes are important for their electrochemical properties, particularly due to the presence of active interfaces within intercalation batteries. The $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ cubic polymorph provides the highest ionic conductivity.^{11,47,51} However, accounting for the Li disorder presents a major computational complexity when creating representative surface structures. Thus, we consider the tetragonal polymorph, which constitutes a distinct ordering of Li sites, as the reference structure for creating our surface models.

Figure 2 depicts the atomic arrangement of the Li-terminated (010) surface of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, highlighting the significant reconstruction of the Li and O layers, respectively. The dotted lines in Figure 2 are a guide for the eye to illustrate the loss of

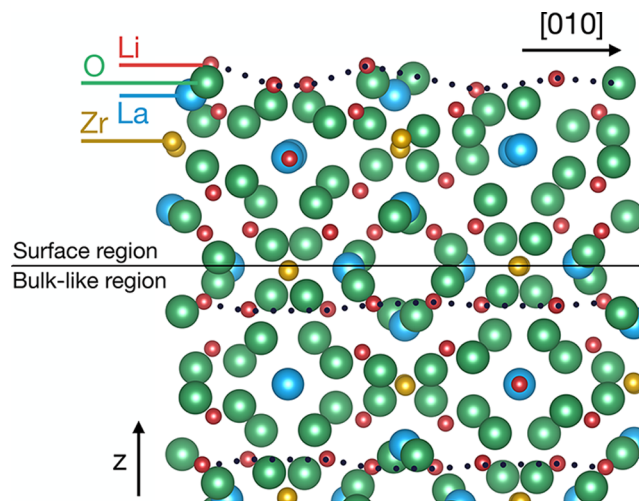


Figure 2. Side view of the nonstoichiometric (010) Li-terminated surface of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. Li atoms are in red, O in green, La in blue, and Zr in gold. Solid lines identify the arrangement of each atom plane along the nonperiodic z axis. The black line marks the separation between the bulk-like region from the surface region. The black dotted lines are guides for the eye to highlight the change in the local Li symmetry upon surface reconstruction.

symmetry of the Li environment at the surface compared to the bulk region. Figure 2 shows that La layers overlap with “rumpled” oxygen layers, which help to stabilize La-terminated surfaces, as discussed in the following paragraphs. In the case of Zr ions, the oxygen coordination environment in the surface slab shows insignificant deviation from the octahedral coordination within bulk $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, in qualitative agreement with the lack of surface reconstruction observed in ZrO_2 .⁵²

It is known that for a given Miller index several surface terminations may be possible since the bulk can be cleaved at different planes, as shown in Figure 2. The relative stability of each surface model is defined by their surface energy (γ , eq 1). Figure 3 depicts the computed γ values of a number of

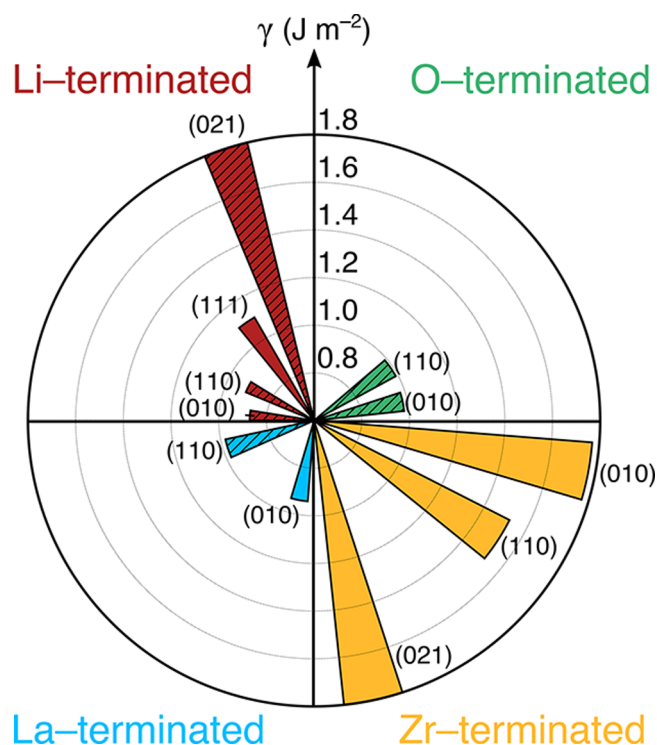


Figure 3. Surface energies γ (J m^{-2}) of La (blue), Li (red), O (green), and Zr (yellow) terminated surfaces of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. Hatched bars indicate nonstoichiometric surfaces, whose surface energies are derived using the chemical potentials from Figure 1b. The chemical potentials of Li, La, and Zr are fixed by Li_2O , La_2O_3 , and Zr metal, respectively, corresponding to reducing conditions (details in section S2 of Supporting Information).

stoichiometric and nonstoichiometric La-, Li-, O-, and Zr-terminated surfaces of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. Nonstoichiometric surfaces refer to surfaces where the stoichiometry deviates in composition from the bulk. The surface energies of symmetry-related Miller index surfaces (e.g., (100) \approx (010) \approx (001)) are detailed in Table S2. As introduced in section S2 of the Supporting Information, the chemical potentials, μ_i , for calculating γ of nonstoichiometric surfaces are set to reducing conditions (i.e., $\mu_{\text{La}} \approx \mu_{\text{La}}$ in La_2O_3 , $\mu_{\text{Li}} \approx \mu_{\text{Li}}$ in Li_2O , and $\mu_{\text{Zr}} \approx \mu_{\text{Zr}}$ in Zr metal); see Figure 1b and section 1 of the Supporting Information.

Figure 3 shows three main features: (i) Zr-terminated surfaces show the highest surface energy γ ($>1.5 \text{ J m}^{-2}$); (ii) certain Li-terminated surfaces possess significantly lower γ ($\sim 0.87 \pm 0.02 \text{ J m}^{-2}$ for the (010) surface), in good agreement with previous work;⁴⁸ (iii) La- and O-terminated surfaces show

similar surface energies, as indicated by γ 0.98 J m^{-2} and 0.99 J m^{-2} for the La- and O-terminated (110) surfaces, respectively.

Although the surface structures are obtained from the tetragonal phase, we find identical surface energies for symmetry inequivalent surfaces (see Table S1 and Figure S1). For example, the surface energy ($\sim 1.77 \text{ J m}^{-2}$) of the Zr-terminated (010) surface is identical to the (001) and (100) surfaces, which is typically not found for tetragonal structures. This suggests the similarity between the tetragonal and cubic phases of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ and indicates that the Li ordering, which affects the relative stability of the bulk tetragonal and cubic phases, has only a negligible impact on the relative symmetry and energetics of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ surfaces. Notably, the c/a ratio exhibited by the tetragonal phase (~ 0.96 from experimental lattice constants, see section S2 of Supporting Information) signifies the small tetragonal distortion in $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$.

Effects of Oxygen Environment and Temperature on Surfaces. With the aim of understanding the interplay between compositional and temperature effects on the morphology of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, we now move our attention to trends of surface energy as a function of temperature and oxygen composition. To include temperature dependence in our model, we apply a thermodynamic framework (detailed in the Method section) that connects changes in the O_2 chemical potential, μ_{O_2} , directly to temperature.⁵³ This approximation is valid as the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ electrolyte is in contact with an oxygen environment during its synthesis and sintering.

With $\mu_{\text{O}} = \frac{1}{2}\mu_{\text{O}_2}$, μ_{O} sets the surface energy of nonstoichiometric surfaces, as indicated in eq 2. Note that under both oxidizing and reducing conditions (section S2 of Supporting Information), the chemical potentials of La and Li are set by La_2O_3 and Li_2O , respectively. All the nonstoichiometric surfaces studied here are either oxygen rich or poor (see Method section). High μ_{O} (or μ_{O_2}) represents low-temperature situations and a highly oxidative environment, where oxygen molecules “condense” on the surfaces of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. In contrast, higher temperatures (i.e., more negative μ_{O}) signify reducing conditions, where oxygen atoms become volatile and leave the surface as O_2 gas, which is equivalent to $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ being in equilibrium with Zr metal.

Figure 4 shows the variation of the surface energy for a number of nonstoichiometric surfaces as a function of temperature, or its equivalent μ_{O} , corresponding to an oxygen partial pressure of 1 atm.

A number of important observations can be drawn from Figure 4. (i) The Li-terminated (010) surface has the lowest γ (as in Figure 3) and the La-terminated (010) stoichiometric surface has the highest γ for temperatures higher than 25°C . The negative slope of each line signifies that all the surfaces are oxygen deficient. While studying nonstoichiometric surfaces, we have focused on La, Li, and O deficient scenarios, as they are most likely to develop at high temperatures.^{54,55} In order to maintain the electroneutrality of oxygen-terminated surfaces, oxygen vacancies were introduced to compensate the removal of cations (details are provided in the Method section). (ii) The stability of the Li-terminated (010) surfaces in comparison to other terminations is significant. (iii) At temperatures higher than 300°C , the O-terminated (010) and (110) surfaces become more stable than the (110) Li-terminated surface. This result is also found for the (100), (001), (011), and (101) Li-terminated facets. (iv) Above 750°C , the negative γ of (010)

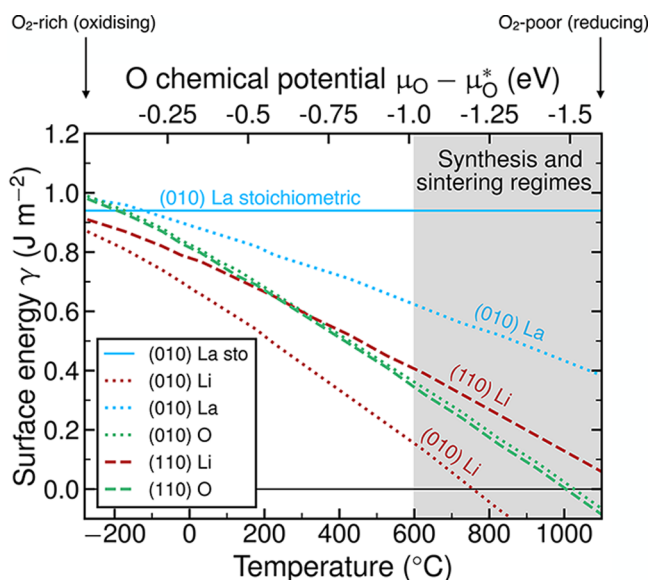


Figure 4. Surface energy γ of La (blue), Li (red), and O (green) terminated $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ surfaces vs temperature and oxygen chemical potential μ_{O} . The blue horizontal line indicates the stoichiometric La-terminated surface energy. The zero (eV) in the μ_{O} scale is normalized against the reference state μ_{O}^* and is detailed in the [Supporting Information](#). μ_{O} near 0 eV relates to oxygen-rich (or oxidizing) regimes, whereas more negative oxygen chemical potentials are oxygen-poor (or reducing) conditions. The gray shading marks the experimental temperature window for synthesis and sintering of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$.¹¹ The chemical potentials of Li and La are fixed by Li_2O and La_2O_3 , respectively, while μ_{O} is allowed to vary.

Li-terminated surface (as seen in [Figure 4](#)) is indicative of the instability of bulk $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ and may be linked to the melting of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles.

Environment Dependent Particle Morphologies. By combining our surface energies of various surface facets at distinct chemical compositions ([Figures 3](#) and [4](#)), we can implement the Wulff construction to derive the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ equilibrium particle morphology at synthesis conditions.

[Figure 5](#) depicts the change of the particle equilibrium morphology as a function of temperature.

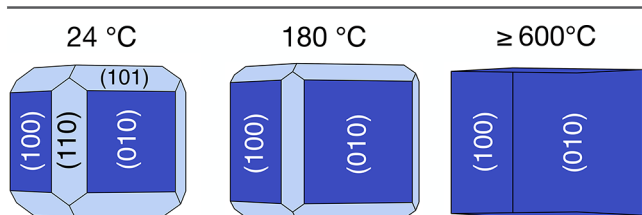


Figure 5. Variation in the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ equilibrium morphology with increasing temperature. The particles are expected to be Li-terminated, as suggested in [Figure 4](#). Labels identify the surface planes of interest.

At room temperature ($\sim 24^\circ\text{C}$), the equilibrium $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particle morphology is dominated by the (001), (101), and (110) surfaces. For temperatures greater than 600°C (and $< 750^\circ\text{C}$), $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles should assume a cubic shape dominated by the (100) and (010) surfaces, as seen in [Figure 5](#).

At 24°C and intermediate temperatures ($\sim 180^\circ\text{C}$), the (110) Li-terminated surface contributes to the overall particle shape. However, an increase in oxygen composition on the

surface of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles will be also observed, as shown by the increased stability of the (110) oxygen-terminated surfaces over (110) Li-terminations, as seen in [Figure 4](#) at temperatures above 300°C .

Tuning the Synthesis Conditions of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. We now examine the surface phase diagram obtained by varying the chemical composition of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. This analysis contributes to understanding the experimental synthesis conditions to achieve the desired chemical composition of the particle surfaces.

Computing a complete surface phase diagram represents a formidable exercise given the large compositional space for the nonstoichiometric terminations accompanied by the large number of atomic arrangements of partially occupied terminating layers. Thus, we limit the discussion of the surface phase diagram to the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ surfaces in [Figure 3](#). Li-rich and Li-poor conditions correspond to Li_2O (reducing conditions) and $\text{Li}_6\text{Zr}_2\text{O}_7$ (oxidizing conditions), respectively, while Zr-rich is equivalent to Zr metal (reducing) and Zr-poor to O_2 gas (oxidizing).

[Figure 6](#) shows the surface phase diagram at 0 K by varying the Li (μ_{Li}) and Zr (μ_{Zr}) composition. We find that regions of low μ_{Li} and μ_{Zr} are consistently dominated by the (010) O- and La-terminated surfaces. At more positive μ_{Li} and μ_{Zr} (near Li-rich and Zr-rich conditions), the (010) Li-terminated surfaces are stable. In fact, the (010) O- and La-terminated surfaces have similar surface energies ~ 0.94 and $\sim 0.98 \text{ J m}^{-2}$, respectively (see [Figure 3](#)), as the La ions exposed are surrounded by a O sublayer. The segregation of La/O and Li to the surfaces of the particles of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ (at specific μ_{Li} and μ_{Zr}) are schematically shown by the green and violet spheres of [Figure 6](#).

[Figure 6](#) also includes a voltage scale, which relates directly to the Li chemical potential ($V = -\mu_{\text{Li}}/e$). Highly negative μ_{Li} signify high voltages (vs Li/Li^+) and vice versa.

DISCUSSION

To gain realistic insights into the design of solid electrolytes for solid-state batteries, we have performed a thorough first-principles calculation analysis of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ surfaces and its morphologies under various physical and chemical conditions.

Morphology and Composition of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ Particles. [Figure 1b](#) shows that lower surface energies are found for surfaces terminated by cations with lower oxidation states, following the trend $\text{Li}^+ < \text{La}^{3+} < \text{Zr}^{4+}$. This finding relates to electrostatic and geometric factors. By cleavage of a cation-terminated surface, the large disruption of the ideal cation coordination environment results in a high-energy penalty, thus impacting significantly on the relative stability of the surface.

Experimentally,⁵⁶ it is found that La^{3+} and Zr^{4+} ions prefer high oxygen coordination (≥ 6 in the cubic and tetragonal $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ phases), whereas Li^+ can adjust to both octahedral and tetrahedral environments.^{11,57} Li ions can tolerate reduced coordination environments leading to lower surface energies compared to Zr-terminated surfaces, which undergo a reduction in coordination from 6–8 to 4. La-terminated surfaces show low surface energies ($\sim 0.94 \text{ J m}^{-2}$) compared to the Zr-terminated surface, which are explained by the oxygen sublayer stabilizing the partially uncoordinated La atoms and lowering the surface energy (see [Figure S3](#)).

We have identified that surfaces with low Miller indices, e.g., (010) and (110) with Li-rich textures, dominate across a wide

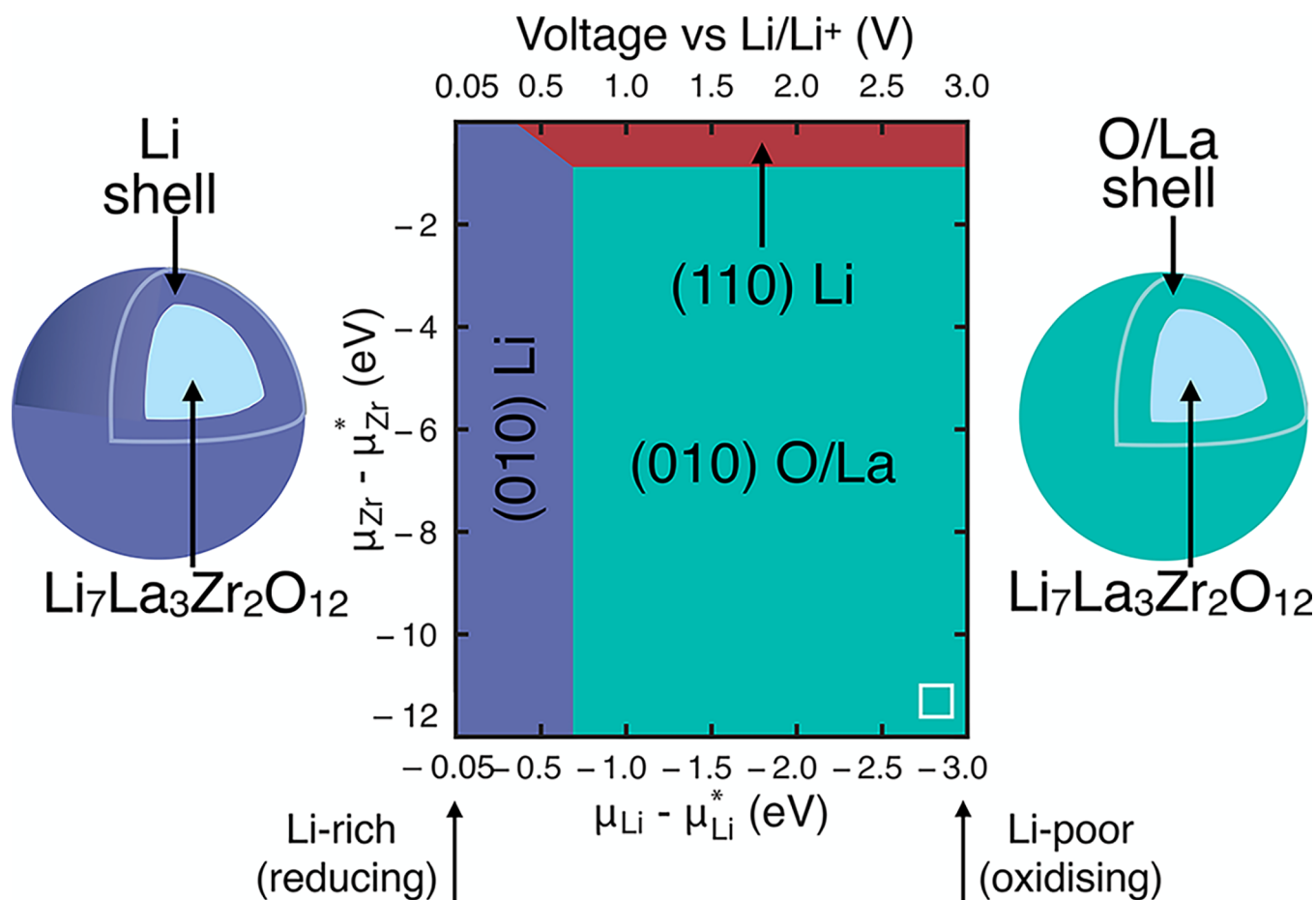


Figure 6. Surface phase diagram at 0 K of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ and schematic representations of particle morphologies at different chemical conditions. Stable surfaces and chemical terminations as a function of μ_{Li} and μ_{Zr} . The white square identifies the compositional Li–Zr conditions where $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ is commonly synthesized. Zr-rich is equivalent to Zr metal (Zr-poor is O_2 gas), whereas Li-rich is Li metal (and Li-poor is $\text{Li}_6\text{Zr}_2\text{O}_7$). The voltage evolution vs Li/Li^* (with $V = -\mu_{\text{Li}}e^-$) is also shown. The chemical potential scales are referenced against the reference states μ_{Li}^* (Li_2O) and μ_{Zr}^* (Zr metal).

range of temperatures and oxygen environments. Li segregation at the surfaces of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles has been demonstrated by neutron depth profiling experiments.³⁹ O-terminated surfaces are also possible, as shown in Figure 6. This may be significant in relation to the recent report of oxygen migration in $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$.⁵⁸

The predicted room temperature morphology of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ is in excellent agreement with a scanning electron microscopy study of a single crystal,⁴⁶ providing credibility to the computed morphologies of Figure 5. However, no specific surface facets were characterized, which we identified here.⁴⁶ We can complement the experimental observations by extending our model beyond the shape of the particles. This is completed by ascertaining the dominant surface facets and the most likely chemical compositions under both reducing and oxidizing conditions.

On the basis of these findings, we speculate that small cations, such as Al^{3+} and Ga^{3+} , doped at Li^+ sites may segregate at the surfaces of the particles. In agreement with our hypothesis, a number of experimental reports demonstrate that Al^{3+} segregates to the grain boundaries of doped $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$.^{55,59,60} We speculate that high-valent cations, such as Ta^{5+} and Bi^{5+} (introduced on the Zr lattice to increase the number of Li vacancies),¹¹ will constitute the core of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles.

Densification and Implications for Ionic Conductivity.

Densification of ceramic oxides via high-temperature (and spark-plasma) sintering is routinely employed to improve the electrolyte ionic conductivity.^{11,45,55} Typically, the interpretation of impedance measurements requires the deconvolution of the total ionic conductivity into three main contributions, namely,^{61–63} intrinsic bulk, grain boundary, and interfacial electrolyte/blocking electrode. While bulk Li-ion transport has been emphasized by both experiment and computation,^{7–9,11,31,32,47,51} grain boundary Li-ion conductivity is much less examined, despite being crucial.^{7–9,11}

The seminal paper on $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ by Murugan et al.⁸ showed significant Li-ion resistance at the grain boundaries (~50% of the total), thus suggesting the relevance of intergranular Li-ion transport.⁶⁴ Ceramic oxides processed at high temperatures containing “volatile” cations, such as Li, including $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, will produce Li deficient bulk materials²⁷ and thus possible Li loss upon sintering treatments. For example, Antolini⁵⁴ showed that sintering of $\text{Li}_x\text{Ni}_{1-x}\text{O}$ ceramic electrodes can promote Li segregation at the particle exterior, thus altering the overall stoichiometry. Loss of Li_2O was observed in the synthesis of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$,^{35,36,55,65} and additional Li_2O is routinely added during its preparation.

In agreement, our prediction in Figure 4 suggests that at high temperatures ($\geq 600^\circ\text{C}$ in the sintering regime) and reducing

conditions, the particle surfaces will show pronounced segregation of Li. Assuming that the stable surfaces computed in this study are representative of the grain boundaries in $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, we speculate that the accumulation of Li ions can impact the Li transport involving grain boundaries.⁶⁴

Engineering the Particle Morphology. On the basis of our predictions, we can propose practical strategies to engineer particle morphologies of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. For example, Figure 6 demonstrates that adding extra Zr and/or Li metals during synthesis may promote Li segregation at the grain boundaries.³⁹ In addition, as indicated in Figure 4, routine high-temperature synthesis of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ promotes reducing conditions (i.e., oxygen-poor conditions) and Li terminated surfaces/particles. Hence low-temperature synthesis (and sintering) protocols should be sought.⁶⁶

From analysis of Figure 6, we speculate that O/La accumulation at the grains is also observed near the operating voltages of typical Li-ion cathode materials (e.g., $\text{LiCoO}_2 \approx 3.8$ V vs Li/Li^+ and $\text{LiFePO}_4 \approx 3.4$ V). In this context, Miara et al.⁶⁷ have shown that $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ remains stable against LiCoO_2 , whereas the analogous interface with LiFePO_4 decomposes forming a protecting Li_3PO_4 interface. Nevertheless, a more recent experimental investigation by Goodenough et al.⁶⁸ showed significant Al^{3+} and La^{3+} migration from Al-doped $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ to LiCoO_2 , and negligible Zr diffusion into LiCoO_2 . In Figure 6, near 3 V we predict La segregation toward the particle surfaces corroborating these experimental findings.

The failure upon short-circuiting of polycrystalline $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ in solid-state devices, utilizing a Li-metal anode, has been linked to dendrite propagation.²⁷ Near 0 V or at the potential of Li metal, we expect the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles to be lithium terminated. In agreement with our results, Li segregation close to a Li-metal anode interface in Al-doped $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ has been recently observed by in situ transmission electron microscopy.³⁸ We speculate that the occurrence of Li at the particle surface and at grain boundaries could indeed set the ideal chemical environment required for Li-dendrite growth and propagation between $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles. In line with our results, Kerman et al.²⁷ proposed that once Li fills a crack in doped $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, fresh electrodeposited Li extrudes to the existing grain boundaries.

Unsurprisingly, the process of dendrite propagation can originate from Li “stuffing” into grain boundaries.²⁷ Thus, the significant accumulation of Li at the surfaces of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles may favor the initial stages of dendrite nucleation and growth along the existing grain boundaries. Further experimental studies are required to verify these hypotheses.

CONCLUSIONS

$\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ is an important solid electrolyte material, but its surfaces and particle morphologies under synthesis and sintering conditions are not fully characterized.

First, by studying the morphology and composition of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles from DFT-based calculations, we have demonstrated the spontaneous segregation of Li toward the particle exterior. Second, we map the compositional changes of the surfaces of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ as a function of temperature and of oxygen chemical pressure. Li segregation to surfaces is the dominant process over a range of temperatures, particularly during high-temperature synthesis and sintering. These findings are significant in relation to the initial stages of Li dendrite

growth. Third, by studying the surface phase diagram of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, we find that Li segregation can be curbed by tuning the ceramic synthesis conditions. We show that synthesis in low temperature oxidizing environments (O-rich, Li-poor and/or Zr-poor) may inhibit Li segregation to the particle surfaces. Finally, we find that particle compositions of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ are altered upon voltage sweeps, with Li segregation at the exterior occurring at the Li-metal anode voltage.

These findings will contribute toward developing strategies for the optimization of the synthesis and operation of promising solid electrolytes for solid-state batteries.

METHOD

Surface Energies and Thermodynamic Framework.

The physical quantity defining stable surface compositions and geometries is the surface free energy γ (in J m^{-2}):

$$\gamma = \frac{1}{2A} \left[G_{\text{surface}} - G_{\text{bulk}} - \sum_i^{\text{species}} \Delta n_i \mu_i \right] \quad (1)$$

where A is the surface area (in m^{-2}) and G_{surface} and G_{bulk} are the surface free energies of periodic surfaces and the reference bulk material, respectively. G_{surface} and G_{bulk} are approximated by the respective computed internal energies E_{surface} and E_{bulk} , accessed by density functional theory (DFT) as described in the Supporting Information. In the case of nonstoichiometric surfaces, the final surface energy depends on the environment set by the chemical potential μ_i for species i and amounting to an off-stoichiometry of Δn_i . Note that Δn_i is negative (positive) if species i is removed (added) to the surface. The chemical potential references μ_i were derived from the computed phase diagram (Figure 1b) at 0 K.

Equation 1 provides γ values at 0 K that are not representative for the operating conditions of solid electrolytes and the synthesis and sintering conditions. For nonstoichiometric surfaces, the approximation chosen to introduce the temperature dependence in the γ values is based on the fact that the surrounding O_2 atmosphere forms an ideal-gas-like reservoir, which is in equilibrium with $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. The effect of temperature is introduced into the definition of γ as follows:

$$\gamma(T) = \frac{1}{2A} \left[E_{\text{surface}} - E_{\text{bulk}} - \sum_i^{\text{species}-\{\text{O}\}} \Delta n_i \mu_i - \Delta n_{\text{O}} \mu_{\text{O}}(T) \right] \quad (2)$$

where μ_{O} is now a temperature dependent quantity and evaluated directly by combining DFT data with experimental values tabulated by NIST/JANAF as⁶⁹

$$\begin{aligned} \mu_{\text{O}}(T) = & \frac{1}{2} \mu_{\text{O}_2}(0 \text{ K, DFT}) + \frac{1}{2} \mu_{\text{O}_2}(0 \text{ K, Exp}) \\ & + \frac{1}{2} \Delta G_{\text{O}_2}(\Delta T, \text{Exp}) \end{aligned} \quad (3)$$

where the $\mu_{\text{O}_2}(0 \text{ K, DFT})$ is the 0 K free energy of an isolated oxygen molecule evaluated with DFT, whereas $\mu_{\text{O}_2}(0 \text{ K, Exp})$ is the 0 K experimental (tabulated) Gibbs energy for oxygen gas. $\Delta G_{\text{O}_2}(\Delta T, \text{Exp})$ is the difference in the Gibbs energy defined at temperature T as $1/2[H(T, \text{O}_2) - H(0 \text{ K, O}_2)] - 1/2T[S(T, \text{O}_2)]$, respectively, as available in the NIST/JANAF tables.⁶⁹ We omitted the partial pressure dependence of the μ_{O_2} term

(i.e., we used $p_{\text{O}_2} = 1 \text{ atm}$) as we expect this contribution to be small, as demonstrated previously.⁵³

Bulk Surface Models. Because of the large number of possible chemical terminations, as a result of the quaternary nature of $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$, the selection of surfaces investigated was only limited to low-index surfaces, such as (100), (001), (101), (111), and (201). We note that some of these surfaces are related by the intrinsic tetragonal symmetry. For example, (100) = (010), as verified by the surface energies in the Supporting Information (see Table S2).

In line with Tasker's classification of oxide surfaces,⁷⁰ only realistic type I surfaces were considered, which are characterized by zero charge and no electrical dipole moment. Nevertheless, these requirements are only satisfied by a limited number of stoichiometric Zr- or La-terminated surfaces with high surface energies.

Because our goal is to rationalize the chemical composition and morphology of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particles, it is crucial to study the Li- and O-terminated surfaces. As a result, type I nonstoichiometric surfaces were generated by selectively removing layers of Zr and/or La and charge-compensated by O removal, as shown schematically in Figure 2. Upon cation removal, charge neutrality is maintained by introducing oxygen vacancies, resulting in the need to investigate a significant number of atomic orderings. We simplify this difficult task by computing with DFT only the 20 orderings with the lowest electrostatic energy, as obtained by minimizing the Ewald energy of each surface using formal charges.⁷¹ This results in the assessment of 420 nonstoichiometric surfaces using DFT. While performing this operation, we enforce symmetry between the two faces of the surfaces. Using this strategy, we identified 21 nonstoichiometric orderings and 11 stoichiometric surfaces that are O-, Li-, La-, and Zr-terminated, respectively, whose surface energies are discussed in Figure 3 and Table S2.

■ ASSOCIATED CONTENT

■ Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.chemmater.8b00649.

Details of first-principles calculations, chemical potentials bounds, surface energies, $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ particle morphologies, and $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ surface reconstruction (PDF)

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Notes

The authors declare no competing financial interest.

The structures of the surfaces identified in this study are available at the repository: https://github.com/pcanepa/MS_LLZO_surface_data or DOI: <https://doi.org/10.5281/zenodo.1219703>.

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